

Student: _____
 Date: _____
 Time: _____

Instructor: Lance Burger
 Course: Math 76 Calculus 2
 Book: California State University, Fresno:
 Math 75: Calculus

Assignment: Team Test 1 (Practice)

1. The velocity of a projectile fired straight into the air is given every half second. Use right endpoints to estimate the distance the projectile travelled in four seconds.

Time (sec)	Velocity (in. / sec)
0	126
0.5	121.1
1.0	116.2
1.5	111.3
2.0	106.4
2.5	101.5
3.0	96.6
3.5	91.7
4.0	86.8

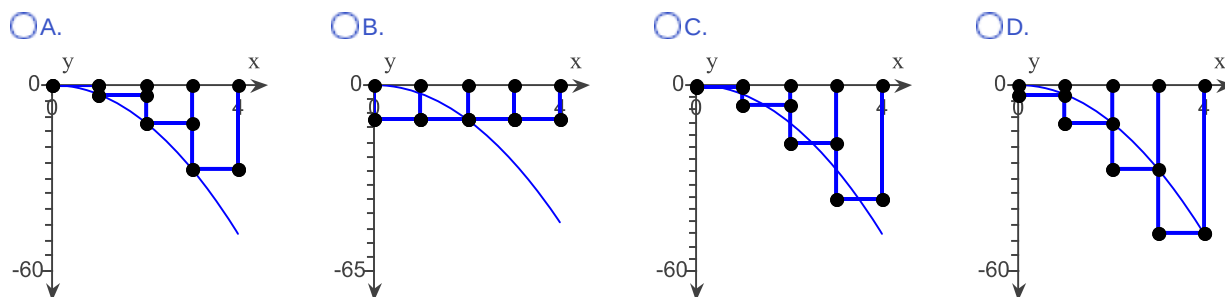
- ☐ A. 870.8 m
☐ B. 435.4 m
☐ C. 415.8 m
☐ D. 831.6 m

2. Use a finite approximation to estimate the area under the graph of the given function on the stated interval as instructed.

$f(x) = x^2$ between $x = 4$ and $x = 8$, using a left sum with four rectangles of equal width

- ☐ A. 174
☐ B. 165
☐ C. 149
☐ D. 126

3. Graph the function $f(x) = -3x^2$ over the interval $[0,4]$. Partition the interval into 4 subintervals of equal length. Then add to your sketch the rectangles associated with the Riemann sum $\sum_{k=1}^4 f(c_k) \Delta x_k$, using the midpoint in the k th subinterval for c_k .



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4. Graph the integrand and use geometry to evaluate the integral.

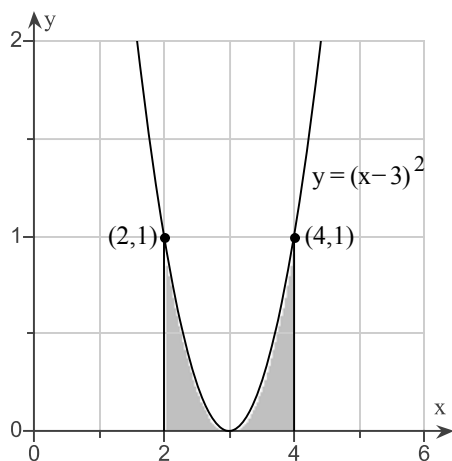
$$\int_{-3}^{10} |x| \, dx$$

- ☐ A. 13
☐ B. $\frac{109}{2}$
☐ C. $\frac{91}{2}$
☐ D. 109

5. Suppose that f and g are continuous and that $\int_3^7 f(x) \, dx = -3$ and $\int_3^7 g(x) \, dx = 10$.
Find $\int_3^7 [f(x) - 5g(x)] \, dx$.

- ☐ A. -53
☐ B. -13
☐ C. 47
☐ D. -65

6. Find the area of the shaded region.



- ☐ A. $\frac{1}{3}$
☐ B. $\frac{5}{3}$
☐ C. $\frac{2}{3}$
☐ D. $\frac{4}{3}$

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7. Find the derivative.

$$\frac{d}{dt} \int_0^{\sin t} \frac{1}{9 - u^2} du$$

- ☐ A. $\frac{\cos t}{9 - \sin^2 t}$
- ☐ B. $\frac{1}{\cos t (9 - \sin^2 t)}$
- ☐ C. $\frac{-\cos t}{9 - \sin^2 t}$
- ☐ D. $\frac{1}{9 - \sin^2 t}$

8. Find the value(s) of x at which the given function equals its average value on the given interval.

$$f(x) = 4 - x^2; [-5, 4]$$

- ☐ A. ± 3
- ☐ B. $\pm \sqrt{6}$
- ☐ C. $\pm \sqrt{7}$
- ☐ D. $\sqrt{5}$

9. Find the average value of the function over the given interval.

$$y = x^2 - 2x + 2; [0, 7]$$

- ☐ A. $\frac{70}{3}$
- ☐ B. 37
- ☐ C. $\frac{29}{4}$
- ☐ D. $\frac{34}{3}$

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10. Evaluate the integral.

$$\int \frac{dx}{x \ln x^4}$$

- ☐ A. $\frac{1}{4} \ln(\ln x^4) + C$
☐ B. $\ln(\ln x^4) + C$
☐ C. $\frac{1}{4} \ln x^4 + C$
☐ D. $\ln x^4 + C$

11. Evaluate the integral.

$$\int \frac{1}{t^2} \sin\left(\frac{4}{t} + 4\right) dt$$

- ☐ A. $\frac{1}{4} \cos\left(\frac{4}{t} + 4\right) + C$
☐ B. $-\cos\left(\frac{4}{t} + 4\right) + C$
☐ C. $-\frac{1}{4} \cos\left(\frac{4}{t} + 4\right) + C$
☐ D. $4 \cos\left(\frac{4}{t} + 4\right) + C$

12. Evaluate the integral.

$$\int e^t \cot(e^t - 6) dt$$

- ☐ A. $\ln|\cos(e^t - 6)| + C$
☐ B. $\ln|\sin(e^t - 6)| + C$
☐ C. $e^t \ln|\sin(t - 6)| + C$
☐ D. $\ln|\sin(t - 6)| + C$

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13. Use the substitution formula to evaluate the integral.

$$\int_0^{\frac{1}{3} \ln \sqrt{3}} \frac{3 e^{3x} dx}{1 + e^{6x}}$$

☐ A. $\frac{\pi}{12}$

☐ B. $-\frac{\pi}{12}$

☐ C. $-\frac{\pi}{6}$

☐ D. $\frac{\pi}{6}$

14. Find the area of the region between the curve $y = 6^{2-x}$ and the interval $0 \leq x \leq 2$ on the x-axis.

☐ A. 36

☐ B. $\frac{36}{\ln 6}$

☐ C. $35 \ln 6$

☐ D. $\frac{35}{\ln 6}$

15. Evaluate the integral by using multiple substitutions.

$$\int \frac{\sin \sqrt{t}}{\sqrt{t} \cos^3 \sqrt{t}} dt$$

☐ A. $\frac{4}{\sqrt{\cos \sqrt{t}}} + C$

☐ B. $-\frac{4}{\sqrt{\cos t}} + C$

☐ C. $\frac{4}{\sqrt{\sin \sqrt{t}}} + C$

☐ D. $-\frac{2}{t^{3/2}} + C$

16. (This problem is worth 5 pts!) Show all work for full credit.
Using the definition of the definite integral as an infinite limit of the Riemann sum, prove that:

$$\int_0^1 x^2 + x \, dx = \frac{5}{6}.$$

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1. C

2. D

3. C

4. B

5. A

6. C

7. A

8. C

9. D

10. A

11. A

12. B

13. A

14. D

15. A

16.